

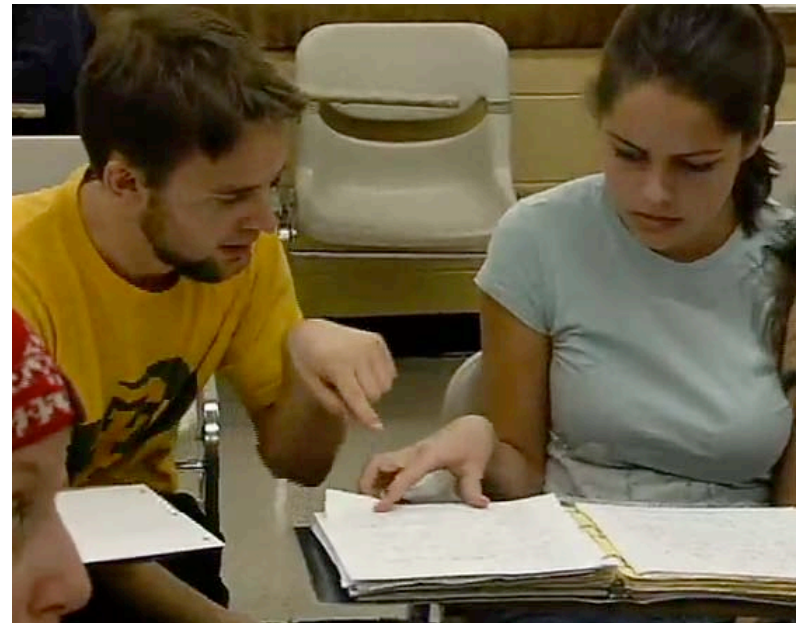
A research-based approach to transforming upper-division E&M

Steven Pollock

+ Kathy Perkins

+ Stephanie V. Chasteen

+ Rachel Pepper



Physics Dept. and Science Education Initiative
University of Colorado at Boulder

CU Physics Education Research

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Noah Podolefsky

And 12 Teaching Fellows in
5 departments

Project in part supported by
CU Integrating STEM

Ph. D. students:

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Non-PER participating faculty

Paul Beale (chair)*

Edward Kinney

Oliver DeWolfe

+ working groups



THE WILLIAM AND FLORA HEWLETT FOUNDATION



American Association
of Physics Teachers

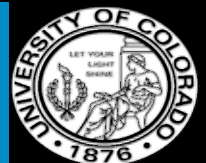
Physics
Teacher
Education



Coalition



APS



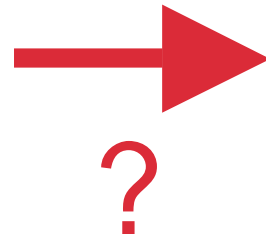
Why Transform E&M I?



Lecture with clickers



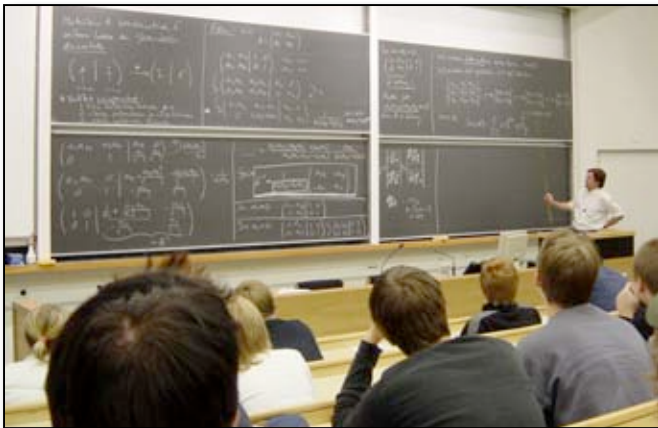
Washington Tutorials



Can our majors learn better from interactive techniques adapted from introductory physics?

What Changed?

- Faculty collaboration
- Explicit learning goals
- Interactive classroom techniques
- Concept Tests
- Modified Homework
- Homework Help Sessions
- Tutorials

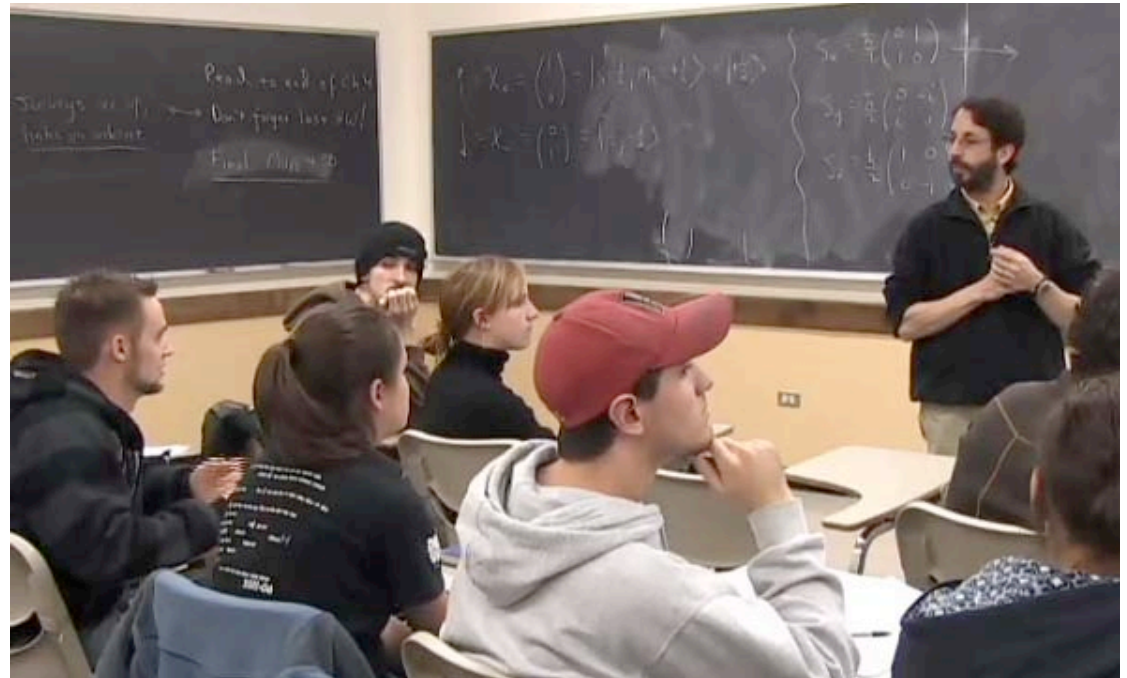


Students debate a concept test

What's special about upper-div?

???

- Intellectually more sophisticated students
- Faculty and student investment & identity
- Complex physics



Learning Goals

- From faculty working group
- Framed course transformations
- Made explicit to students

Students should

... be able to achieve physical insight through the mathematics of a problem

... be able to choose and apply the appropriate problem-solving technique

... demonstrate intellectual maturity

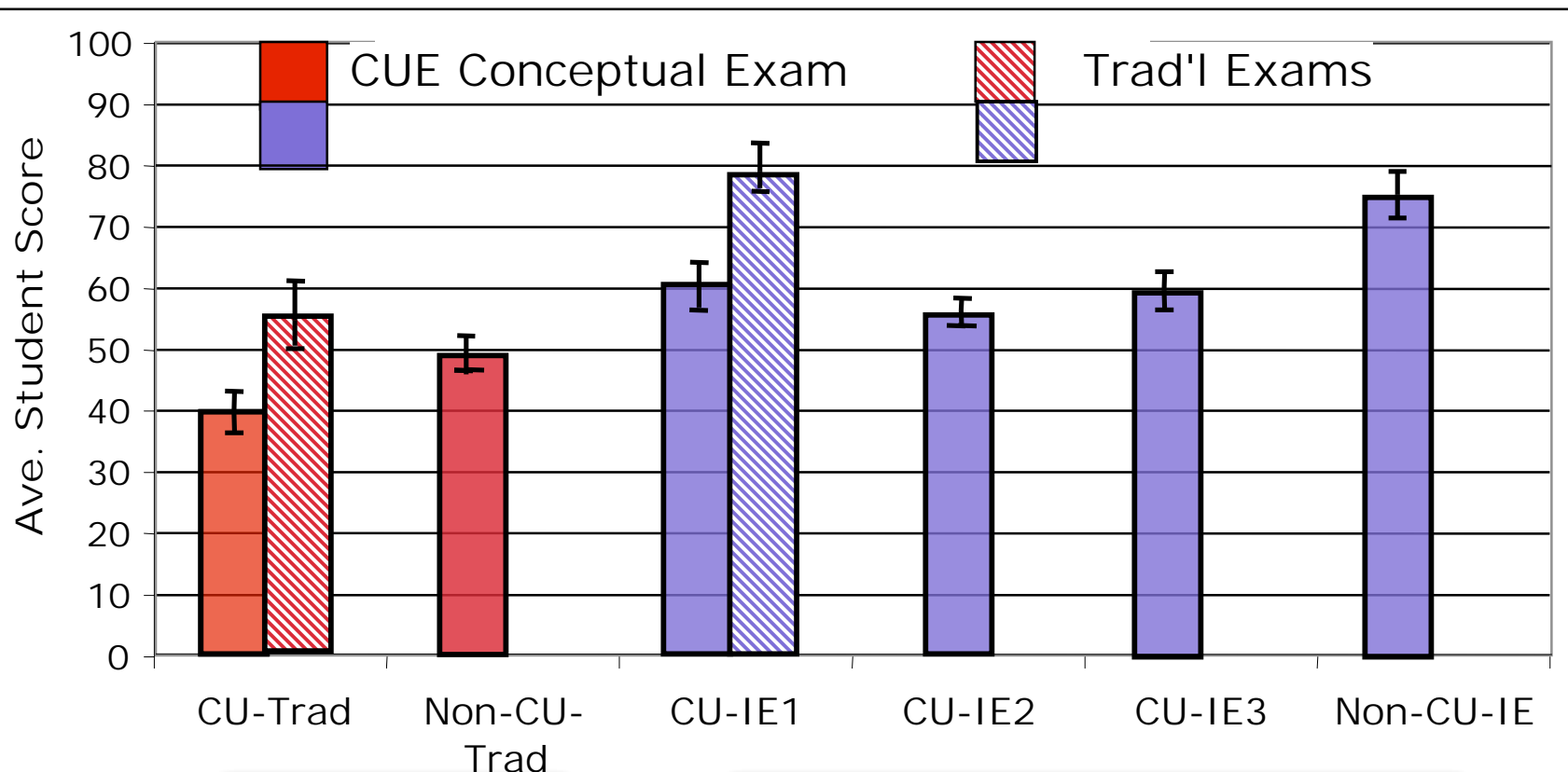


Did it Work? Assessments

- Compared **Traditional** (3 courses) & **Transformed** (4 courses) at CU and elsewhere (N=220).
- Attendance and reported time on homework
- Common **traditional exam questions** (5)
- Developed **Colorado Upper-Division Electrostatics Assessment (CUE)** to gauge progress on learning goals
 - High internal statistical consistency, high inter-rater reliability



Results: CUE and Trad'l Exams



N=220

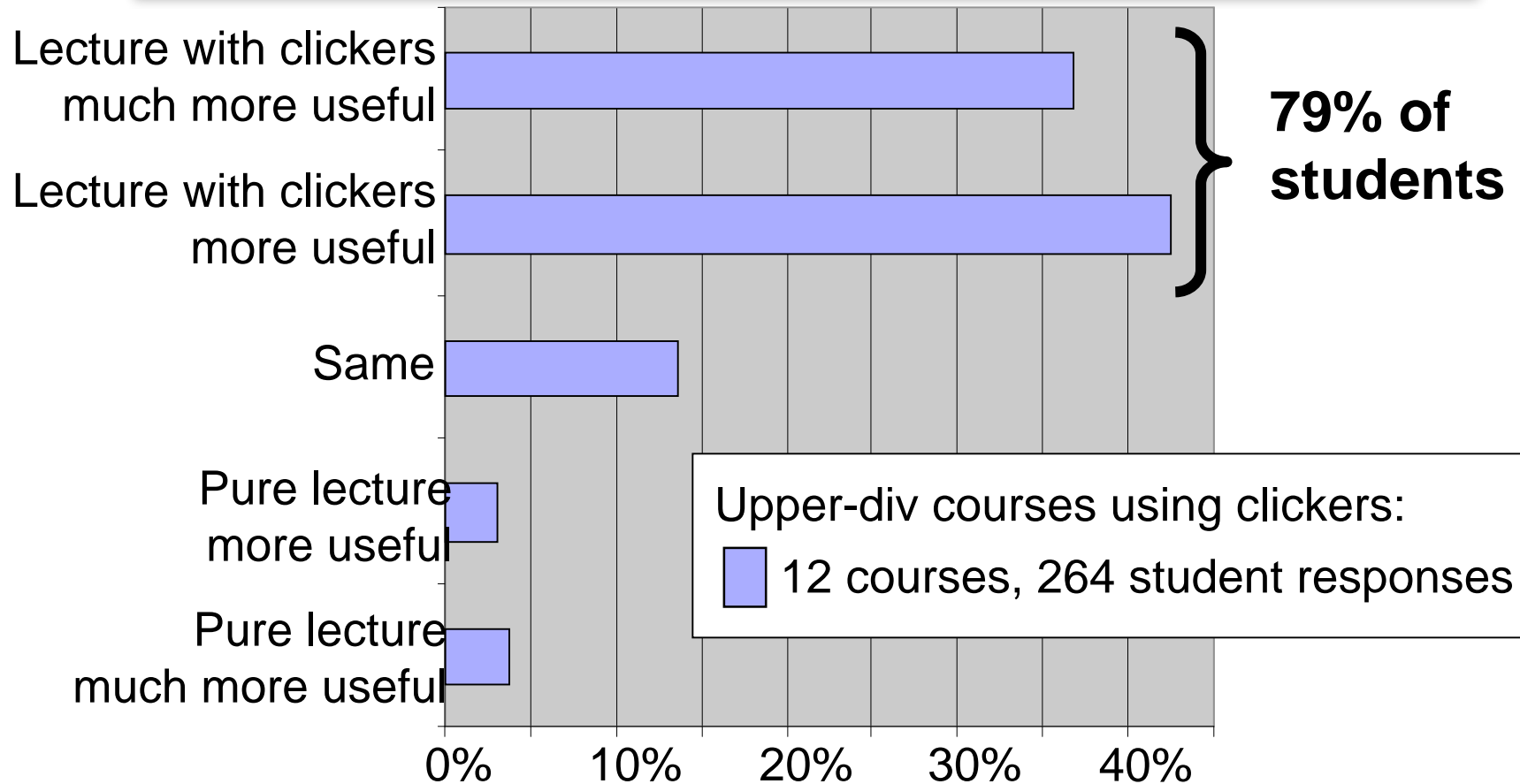
← Trad ⇒

← Transformed ⇒

Students in 4 semesters of Transformations at CU and elsewhere performed significantly better ($p < 0.05$) on all measures

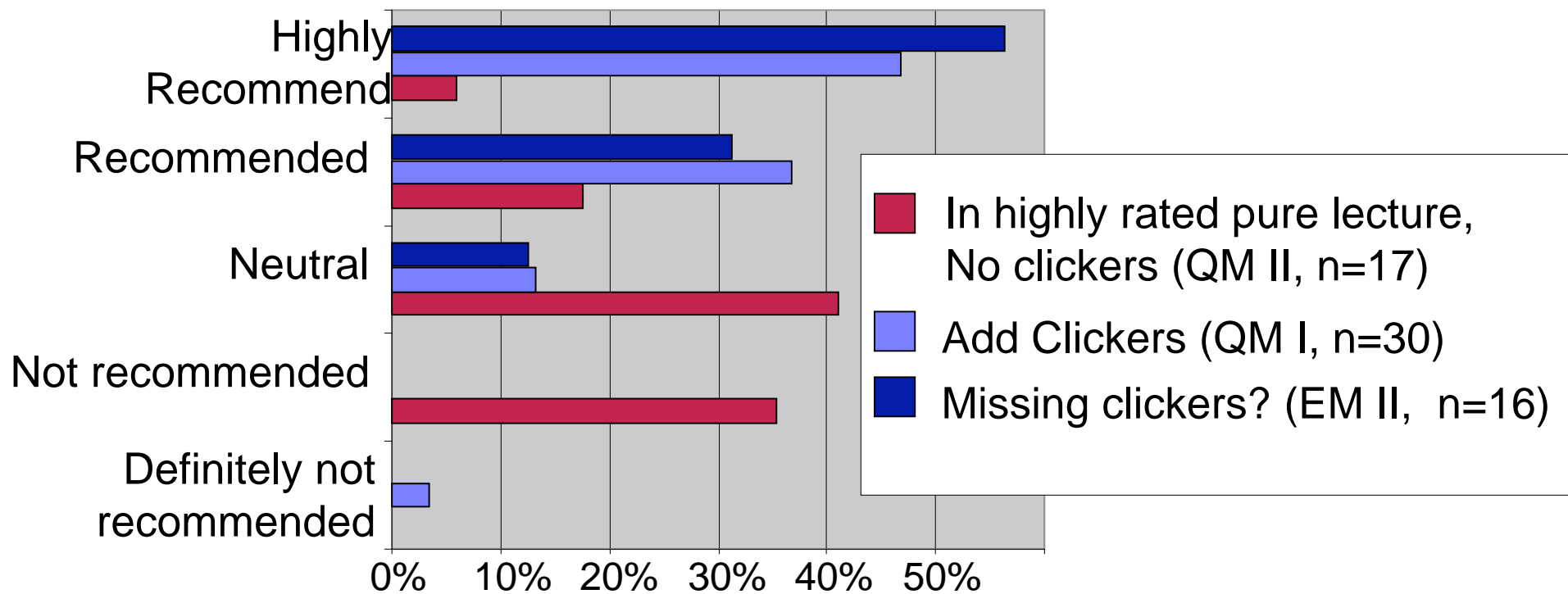
Students Find Clickers Useful

Q: How useful for your learning is the addition of clicker questions compared to pure lecture with no clicker questions?



Student's can't predict value

Q: Would you recommend using clicker questions in upper-level physics courses?



Students' recommendation for implementation

of Qs per lecture: 2-5 [2-3 (62%); 4-5+ (21%)]

Timing: Interspersed with lecture (87%)

Peer-discussion: Allow and encourage (80%)

Preferred response mode:

93% prefer peer discussion as part of response

64% prefer some time for individual thinking prior to peer discussion

N=11 courses, 224 responses

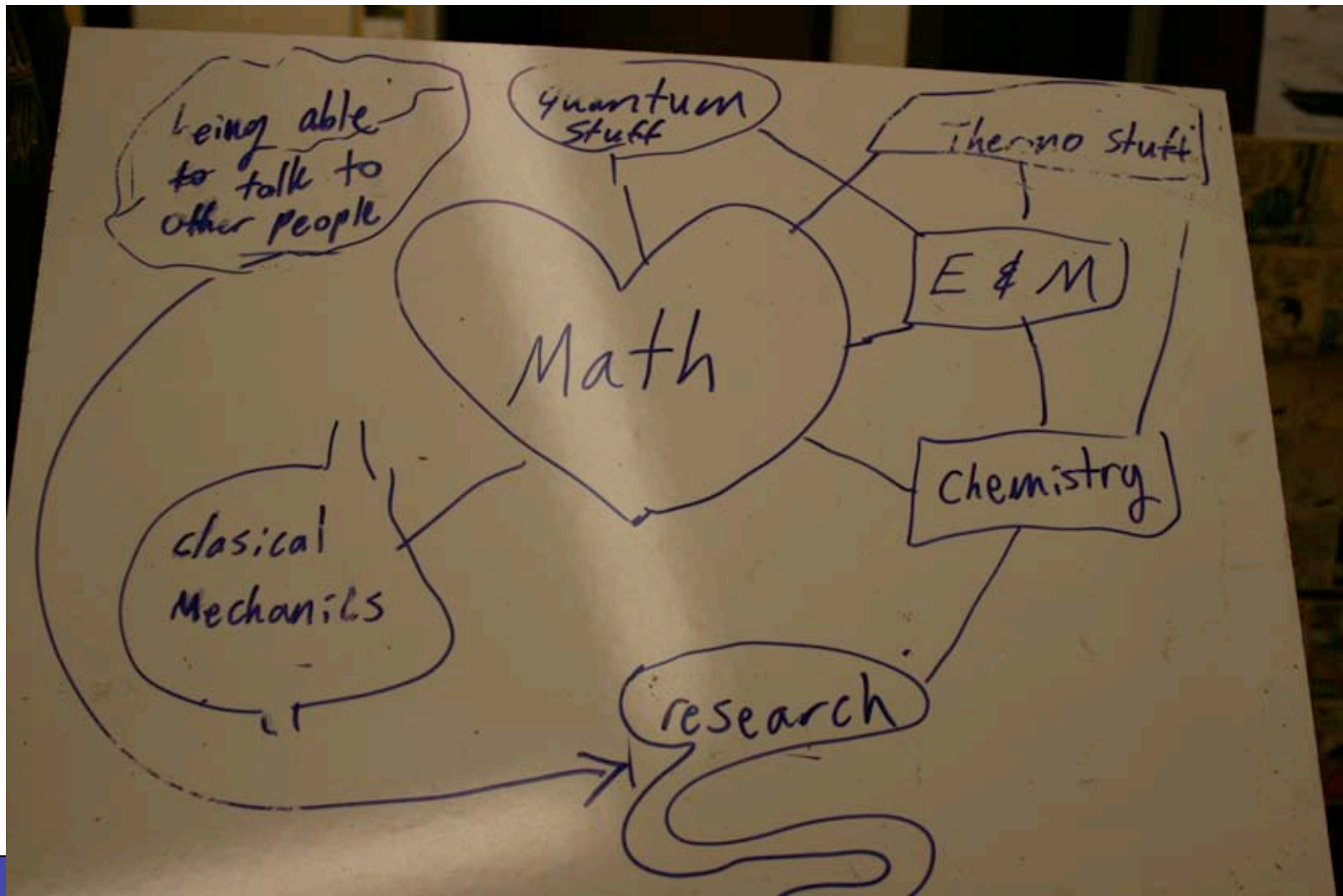


Whiteboard activities

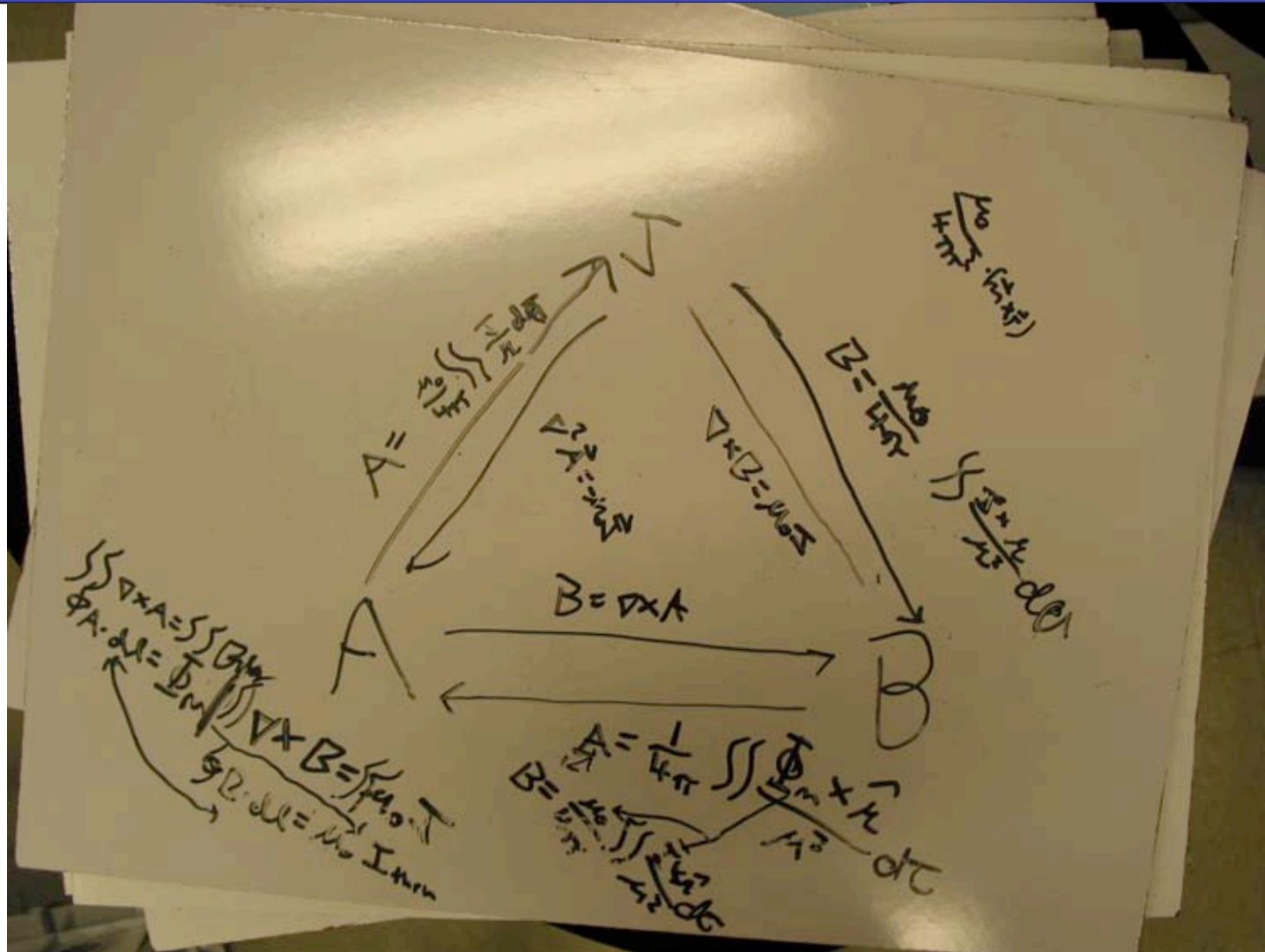
- 1X week
- Uncertain impact
- Uses:
 - Sketch a function (wavefunction or E-field)
 - Concept map of physics
 - Work out an integral or other computation



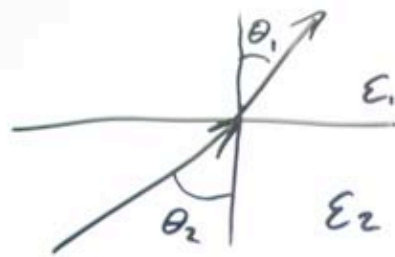
Concept map (whiteboard)



J-B-A triangle (whiteboard)



Boundary conditions for D/E



$$\frac{E_{1\parallel}''}{E_{1\perp}} = \tan \theta_1$$

$$\frac{E_{2\parallel}}{E_{2\perp}} = \tan \theta_2$$

$$\frac{\tan \theta_1}{\tan \theta_2} = \frac{\frac{E_{1\parallel}''}{E_{1\perp}}}{\frac{E_{2\parallel}}{E_{2\perp}}} = \frac{E_2^{\perp}}{E_1^{\perp}} = \frac{E_2 \cos \theta_2}{E_1 \cos \theta_1} = \frac{\frac{D_2 \cos \theta_2}{\epsilon_2}}{\frac{D_1 \cos \theta_1}{\epsilon_1}}$$

$$\frac{\tan \theta_1}{\tan \theta_2} = \frac{\epsilon_1}{\epsilon_2}$$

ϵ higher

Kinesthetic activity

Phys 3310

- You are all positively charged.
- Picture the \vec{E} -field as you enter
- What External work is needed to get to your seat?

Largely built on OSU
(Paradigms) materials

Concept Tests



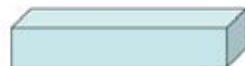
- Allowed students to **discuss & debate challenging, high-level ideas**

An ideal (large) capacitor has charge Q . A neutral *linear* dielectric is inserted into the gap (with given dielectric constant)

Where is D discontinuous?

- i) near the free charges on the plates
- ii) near the bound charges on the dielectric surface

+Q



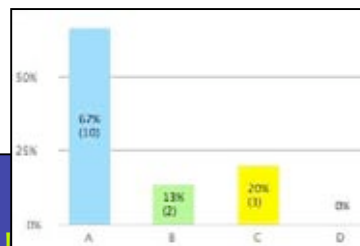
-Q

- A) i only B) ii only C) i and ii ONLY
 D) i and ii but also other places E) none of these/other

Which of the following *could* be a static physical E-field in a small region?



- A) Both B) Only I C) Only II D) Neither



Homework

- Traditional HW problems were modified
- Sense-making, real-world context, estimations, and more.

Q2. DIVERGENCE AND CURL

Consider a field $\mathbf{E} = c \frac{\vec{\mathbf{r}}}{r^2}$ (which is NOT the field from a point charge at the origin, right?!!)

- a) **Sketch it.** Calculate the divergence *and* the curl of this \mathbf{E} field. Test your answers by using the divergence theorem and Stoke's theorem. **Is there a delta function at the origin like there was for a point charge field, or not?**
- b) What are the units of c ? **What charge distribution would you need to produce an \mathbf{E} field like this? Describe it in words as well as formulas. (Is it physically realizable?)**

Sample HW problem aligned with learning goals. Non-traditional portions in bold.



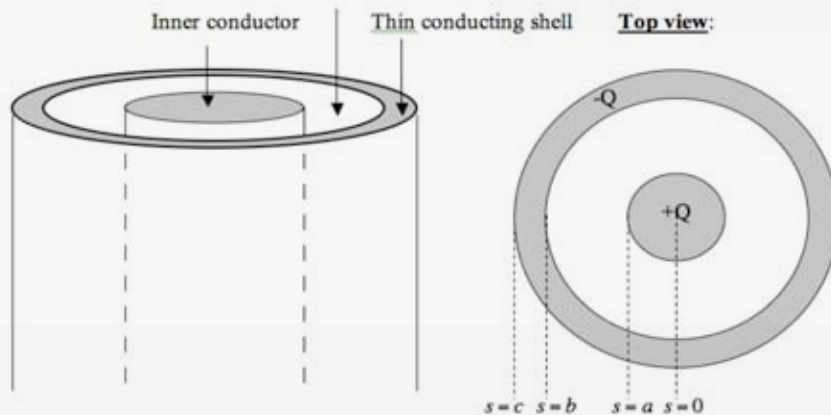
Tutorials & HW Help Sessions

Optional help sessions (2) and tutorials (1) each week



Part 1 – Conceptually Understanding Conductors

A coax cable is essentially one long conducting cylinder surrounded by a conducting cylindrical shell. Draw the charge distribution (little + and - signs) if the inner conductor has a total charge $+Q$ on it, and the outer conductor has a total charge $-Q$. Be precise about exactly where the charge will be on these conductors, and how you know.



Portion of a CU tutorial

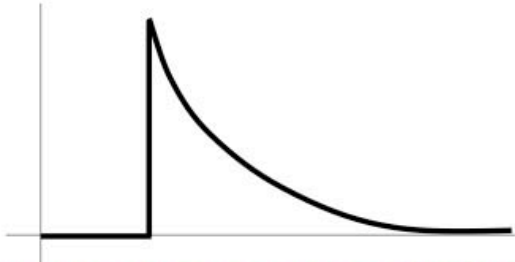


Example Questions

SP

- Conceptual
- Math/Physics connection
- Application of ideas
- Step in calculation, proof, derivation

2.44



Could this be a plot of $|E|(r)$? Or $V(r)$? (for SOME physical situation?)

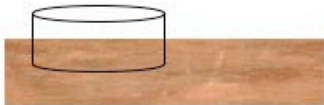
A) Could be $E(r)$, or $V(r)$
B) Could be $E(r)$, but can't be $V(r)$
C) Can't be $E(r)$, could be $V(r)$
D) Can't be either E) ???



Questions: Fundamentals

2.34

We have a large copper plate with uniform surface charge density σ . Imagine the Gaussian surface drawn below. Calculate the E-field a small distance s above the conductor surface.



- A) $|E| = \sigma/\epsilon_0$
- B) $|E| = \sigma/2\epsilon_0$
- C) $|E| = \sigma/4\epsilon_0$
- D) $|E| = (1/4\pi\epsilon_0)(\sigma/s^2)$
- E) $|E| = 0$

30% correct (60% voting "C") before discussion - then 60% correct

Freshmen: 45%, 60% next day

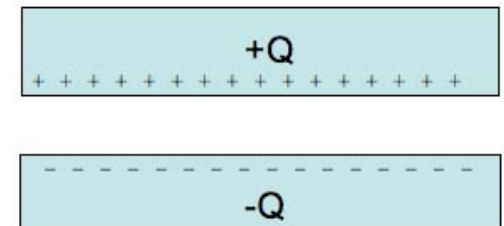


UD: 60 % correct

2.49

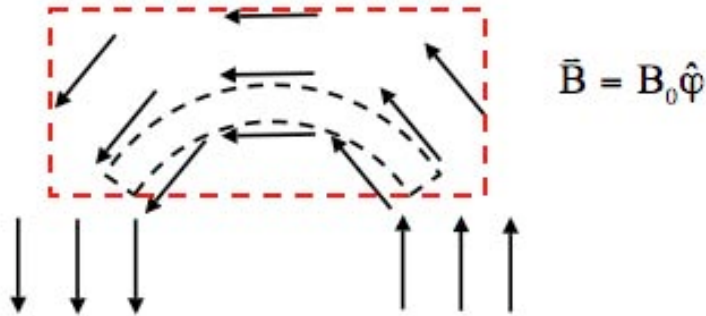
Given a pair of very large, flat, conducting capacitor plates with surface charge densities $\pm\sigma$, what is the E field in the region between the plates?

- A) $\sigma/2\epsilon_0$
- B) σ/ϵ_0
- C) $2\sigma/\epsilon_0$
- D) $4\sigma/\epsilon_0$
- E) Something else



Questions: Conceptual

5.17
b If the arrows represent a B field (note that $|B|$ is the same everywhere), is there a nonzero J (perpendicular to the page) in the dashed region?



- A. Yes
- B. No
- C. Need more information to decide

74% correct
("Need more info")

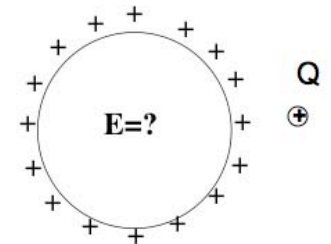


freshmen: 33%
ud: 80% correct →

2.29
alt

A point charge Q is placed outside a uniformly charged shell of charge (uniform σ)

What is the electric field *inside* the sphere?



- A: 0 everywhere inside
- B: non-zero everywhere in the sphere
- C: Something else
- D: Not enough info given

Questions: “Next step”

- **Next step**
 - Derivation
 - Proof
 - Calculation

84% correct

In general, given Hermitian operators A and B , and a state ψ , (and with the usual notation $\langle A \rangle = \langle \psi | A | \psi \rangle$) what can you say about

$$\langle \psi | \langle A \rangle B | \psi \rangle = ?$$

- A) $\langle AB \rangle$
- B) $\langle BA \rangle$
- C) $\langle B \rangle \langle A \rangle$
- D) MORE than one of these is correct!
- E) NONE of these is, in general, correct!

Part of generalized uncertainty principle proof in QM



Questions: "Application"

- **Application**

- Of abstract idea
- To new situation
- To real-world
- Variations on a theme

5.8

A "ribbon" (width a) of surface current flows (with surface current density K)
Right next to it is a second identical ribbon of current.

Viewed collectively, what is the new total surface current density?

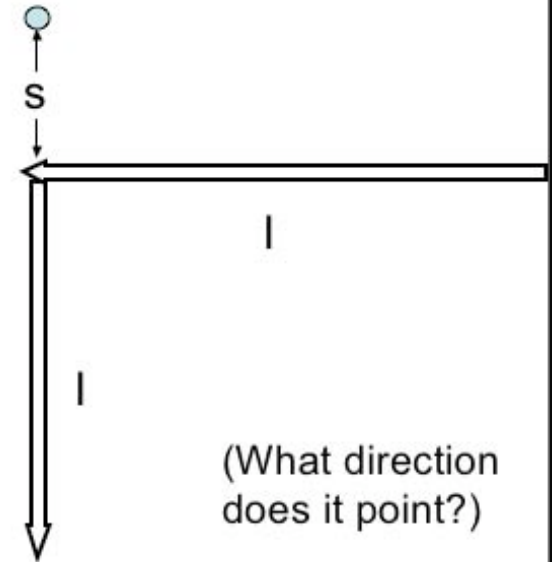
- A) K
- B) $2K$
- C) $K/2$
- D) Something else



5.14

What is B at the point shown?

- A) $\frac{\mu_0 I}{\pi s}$
- B) $\frac{\mu_0 I}{2\pi s}$
- C) $\frac{\mu_0 I}{4\pi s}$
- D) $\frac{\mu_0 I}{8\pi s}$
- E) None of these



(What direction does it point?)

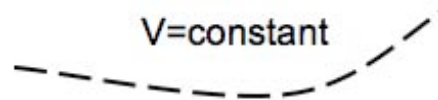
Mostly correct,
but good discussions

Questions: Math/Physics

- **Math/Physics**

- Apply mathematics to a physical situation
- Translate physical situation into math

The voltage is constant everywhere along a line in space.



You can conclude that :

- A) The E-field has constant magnitude along that line.
- B) The E-field is zero along that line.
- C) You can conclude nothing at all about the magnitude of **E** along that line.

Understanding
 $E = -(\text{grad})V$



Research on student difficulties

Research-based

- Tutorials
- Clicker Questions
- Homeworks
- Class activities

Research-validated

- Consensus learning goals
- CUE instrument
- interviews and class observations

*reflective
development*



Research on student difficulties

Research-based

- Tutorials
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*reflective
development*

Research-validated

- Consensus learning goals
- CUE instrument
- interviews and class observations

and next:

- pre/post Tutorial assessments



pre-tests

Week 4 puzzler

Page 1 of 1

Survey timer

Please type your name in the form: Last, First:

Time remaining:

0:09:47

- collaboration w. UW
- weekly online pre-tests
- followup post-tests before exams
- *investigate student difficulties and reasoning*



pre-test (post lecture)

In a bank heist gone awry, you and a friend are stuck inside a (conducting) metal bank vault. Somewhere completely inside the solid metal door is a lock-release mechanism that will trip if you drill through it. This mechanism is a positively charged insulator. Can you and your friend figure out the right place to drill by measuring the E-field inside the safe? Please explain your reasoning.

80%

Can your third accomplice, who is outside the safe, figure out where to drill by measuring the electric field outside the safe? Please explain your reasoning

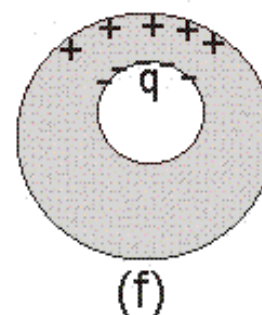
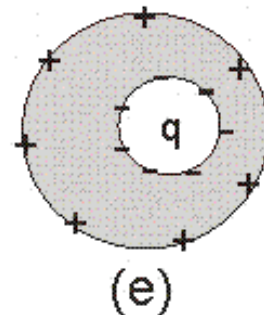
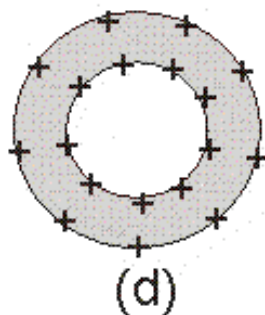
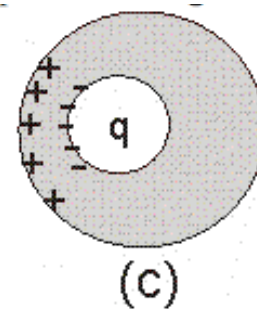
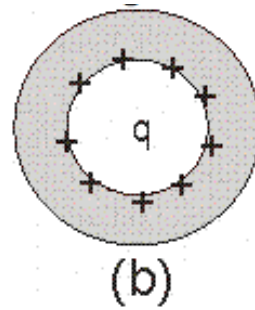
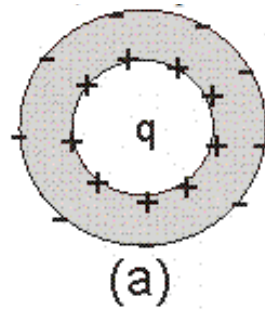
50%



pre-test (post lecture)

Which of the following could be a physically allowable static charge distribution?

Why/why not?



20%

1st posttests just in

By end of term:

- first round for all weeks
- some student interviews likely
- use results to re-write next round and inform Tutorial development



Summary

We are transforming an upper division class:

- Impact on content learning
- Impact on participation

Included faculty (buy-in?)

Developing materials and resources

Developing assessment instruments



Upper-div Clickers at CU

Course	← Sp04 → Sp09 →									
Mech & Math I						★	★			
Mech & Math II							★			★
EM I									★	★
EM II										★
QM I									★	★
QM II									★	
Solid State							★		★	★
Stat Mech	★		★			★	★		★	★
Optics									★	
Grad AMO							★	★		★

➤ 12 non-PER ★ and 2 PER ★ faculty



Questions?

- PER course materials for Quantum and E&M
<http://www.colorado.edu/sei/departments/physics.htm>
- Clicker videos and today's talk at
[STEMclickers.colorado.edu](http://stemclickers.colorado.edu)

<http://per.colorado.edu>

