

# Learning Science and Technology to Understand Your Domain and Improve Student Learning

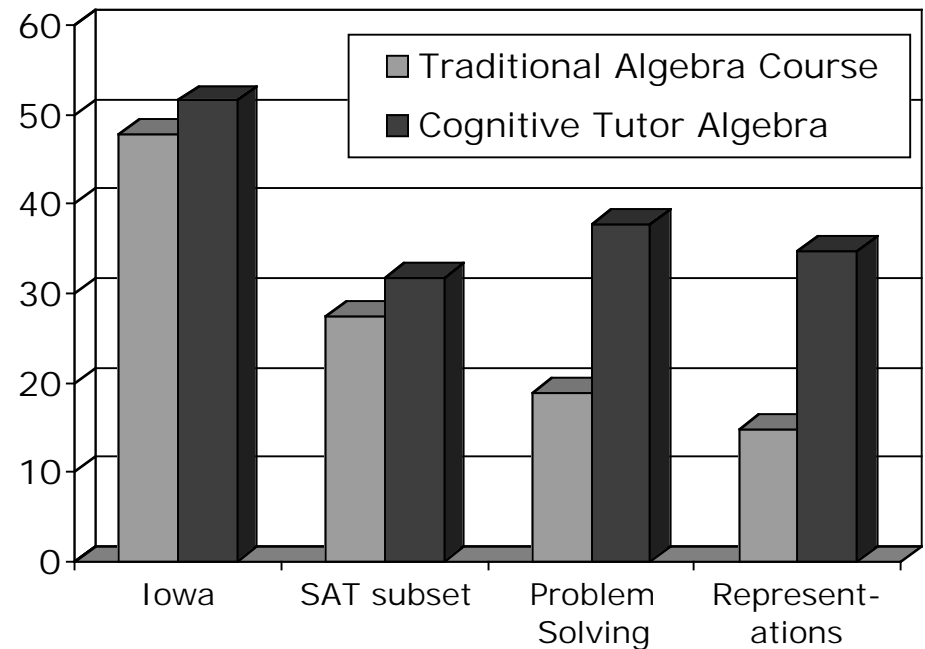
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Human-Computer Interaction &  
Psychology  
Carnegie Mellon University



# Learning Science Success

## *Cognitive Tutor Algebra course*

- Based on ACT-R theory & computational models of student problem solving
- Wide-spread use & evaluation
  - 500,000 students use daily at 2600 schools
  - 8 of 10 full-year field studies demonstrate significantly better student learning



Koedinger, Anderson, Hadley, & Mark (1997).  
Intelligent tutoring goes to school in the big city.

# How do deep structural representations form & facilitate transfer?

## Relevant cognitive theory

- Analogical transfer via schema abstraction
  - Gick & Holyoak, 83; Gentner, Loewenstein et al, 09
- Implicit elements: Perceptual chunking, probabilistic grammars
  - Gobet, 02; Goldstone, Landy, & Son, 09
  - Lari & Young, 90; Li, Cohen, Koedinger, 10
- Explicit elements: Sense making, explanation-based learning, comparison of contrasting cases
- A cog architecture that can flexibly recombine abstracted knowledge components
  - ACT-R, ICARUS, Soar

# Two Paths To Effective Instructional Improvement

- Performing domain-specific cognitive task analysis
- Applying domain-general principles of learning & instruction

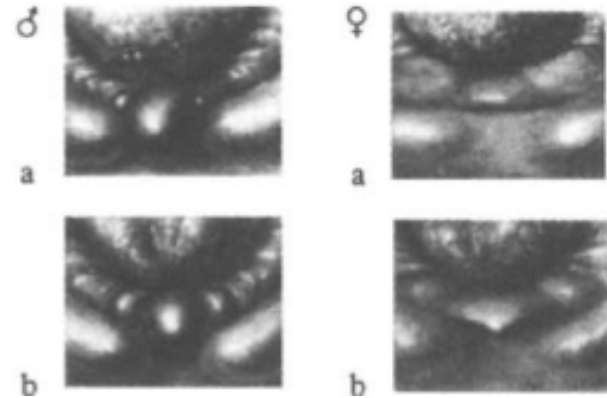
Why is it so tempting to think we know a lot about effective teaching?

- You've had lots of experience with the English language.
- You might say you know English.
- But, do you know what you know?

# Unpacking & repacking expertise: Chick sexing



- Experts don't know, what they know
  - 98% accurate after years of on-the-job training
- Interviews led to design of "pictures in which *critical features* of various types were indicated"
- After just minutes of instruction, novices brought to 84% accuracy!



Male chicken genitals tend to look round and fullish like a ball or watermelon. Here are two examples:



Female chicken genitals can take on two different appearances. They can look pointed, like an upside down pine tree, or flatish. Here are two examples:



# Cognitive Task Analysis

= Knowledge

- Techniques to specify *cognitive structures & processes* associated with task performance
  - Think aloud, structured interviews
  - Newell & Simon: Knowledge-based computer simulations of human reasoning



# Cognitive Task Analysis Improves Instruction

Studies: Traditional instruction vs. CTA-based

- Med school catheter insertion (Velmahos et al., 2004)
  - Sig greater pre to post gain; better with patients on all 4 measures (including needle insertion attempts!)
- Radar system troubleshooting (Schaafstal et al., 2000)
  - CTA group solved 2x malfunctions & in less time
- Spreadsheet use (Merrill, 2002)
  - Post-test: 89% vs. 64% in half of training time
- Lee (2004) meta-analysis: 1.7 effect size!

# Isn't knowledge analysis done for long-standing academic domains?

- Hasn't all this been worked out?
- Surely by now we understand the content of, say,  
Physics?  
or Algebra?

# Difficulty Factors Assessment:

## Discovering What is Hard for Students to Learn

*Which problem type is most difficult for Algebra students?*

### Story Problem

As a waiter, Ted gets \$6 per hour. One night he made \$66 in tips and earned a total of \$81.90. How many hours did Ted work?

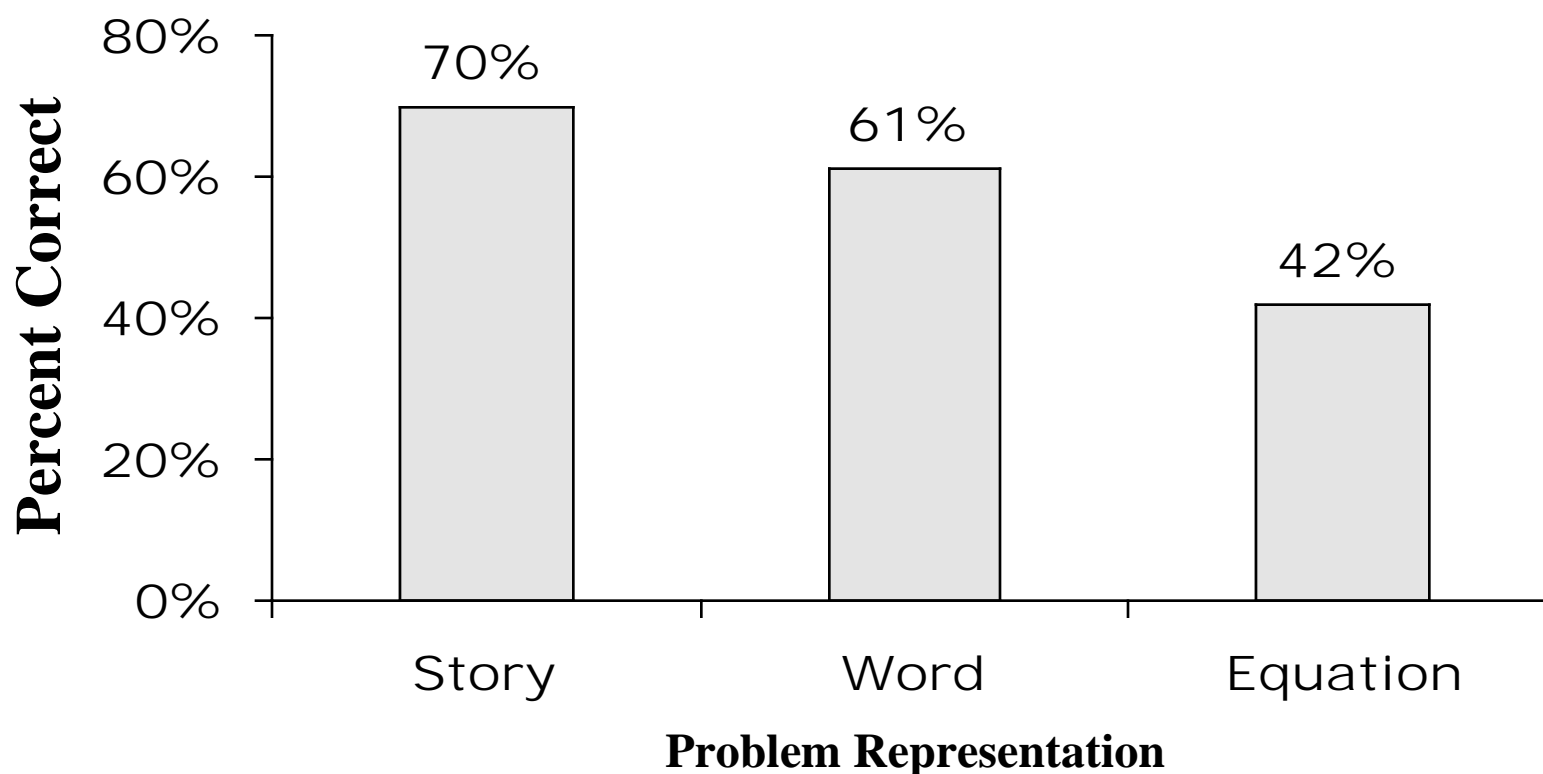
### Word Problem

Starting with some number, if I multiply it by 6 and then add 66, I get 81.90. What number did I start with?

### Equation

$$x * 6 + 66 = 81.90$$

# Algebra Student Results: Story Problems are Easier!



Koedinger, & Nathan (2004). The real story behind story problems: Effects of representations on quantitative reasoning. *The Journal of the Learning Sciences*.

Koedinger, Alibali, & Nathan (2008). Trade-offs between grounded and abstract representations: Evidence from algebra problem solving. *Cognitive Science*.

# Typical textbook strategy

8. After buying donuts at Wholey Donuts, Laura multiplies the number of donuts she bought by their price of \$0.37 per donut. Then she adds the \$0.22 charge for the box they came in and gets \$2.81. How many donuts did she buy?

$$\begin{array}{r} .37x + .22 = 2.81 \\ - .22 \quad - .22 \\ \hline \end{array}$$

$$\begin{array}{r} .37 \overline{) 2.59} \\ \underline{.37} \phantom{0} \\ .22 \phantom{0} \\ \underline{.22} \\ 0 \phantom{0} \end{array}$$

$$\frac{.37x}{.37} = \frac{2.59}{.37}$$

$$x = 7$$

# Informal Strategies

5. Starting with some number, if I multiply it by .37 and then add .22, I get 2.81. What number did I start with?

Handwritten work for problem 5:

$$\begin{array}{r} \text{2.81} \\ \times .37 \\ \hline 2.59 \\ + .22 \\ \hline 2.81 \end{array}$$

$$\begin{array}{r} \text{1.85} \\ \times .37 \\ \hline 1.85 \\ + .22 \\ \hline 2.07 \end{array}$$

Vertical numbers on the left: 2.81, 2.59, 2.81, 2.07

$$\begin{array}{r} .37 \\ \times 2 \\ \hline .74 \\ + .22 \\ \hline .96 \end{array}$$

Handwritten work for problem 5 (circled):

$$\begin{array}{r} .37 \\ + .22 \\ \hline .59 \end{array}$$

$$\begin{array}{r} 2.81 \\ \times 6 \\ \hline 16.86 \end{array}$$

The number is 2

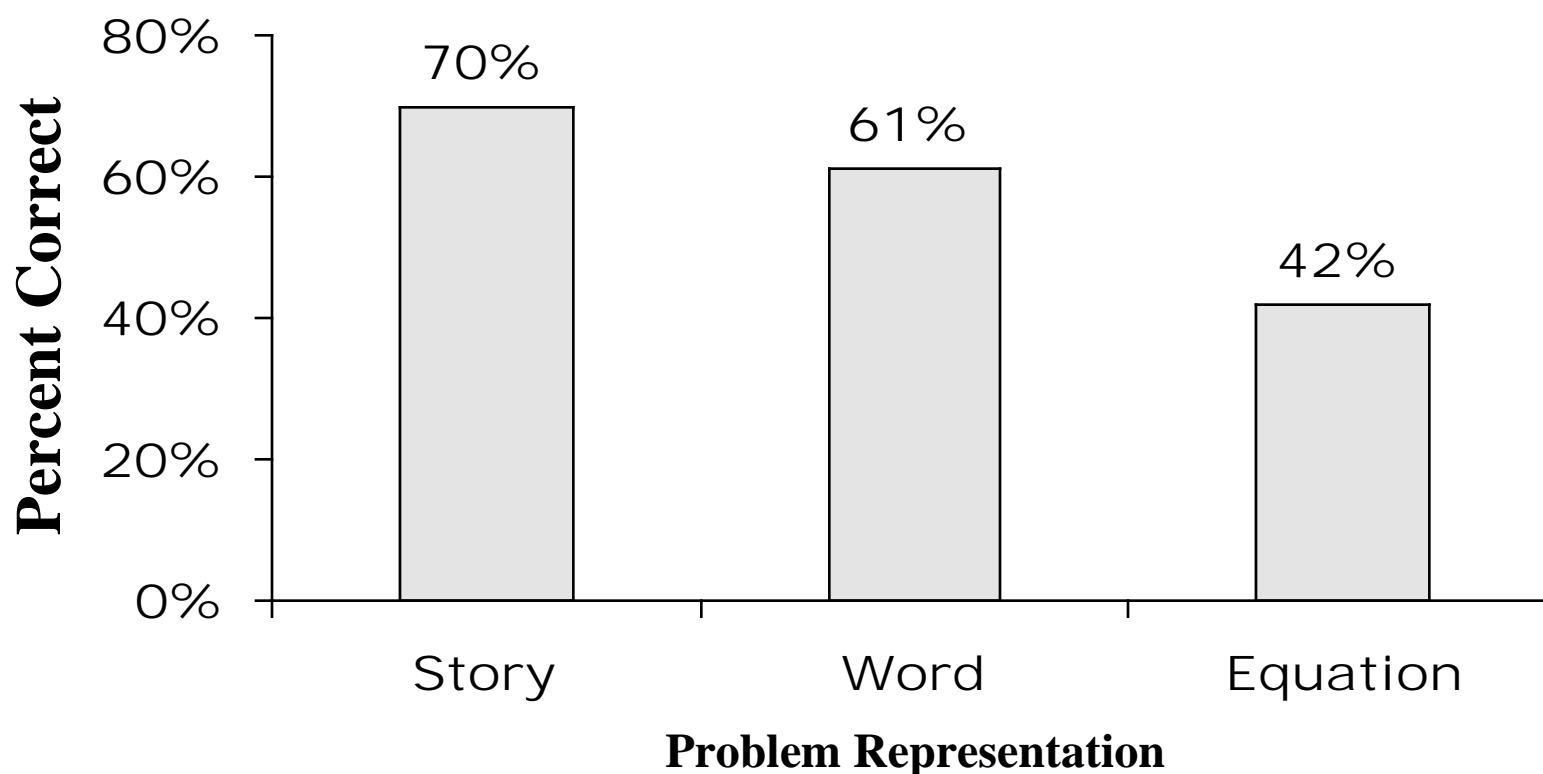
2. After hearing that Mom won a lottery prize, Bill took the amount she won and subtracted the \$64 that Mom kept for herself. Then he divided the remaining money among her 3 sons giving each \$26.50. How much did Mom win?

mom won  
143.50

$$\begin{array}{r} 179.50 \\ + 64.00 \\ \hline 243.50 \end{array}$$

$$\begin{array}{r} 26.50 \\ \times 3 \\ \hline 79.50 \end{array}$$

# Algebra Student Results: Story Problems are Easier!



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The foreign language of algebra:  
Difficulties with syntax & semantics

2. Solve for x:

$$x \times 25 + 10 = 110$$

$$\begin{array}{r} -10 \\ \hline \end{array}$$

$$x \times 15 = 110$$

$$\begin{array}{r} -15 \\ \hline \end{array}$$

$$x = 95$$

2. Solve for x:

$$x * .37 + .22 = 2.81$$

$$\begin{array}{r} .37 \\ +.22 \\ \hline .59 \end{array}$$

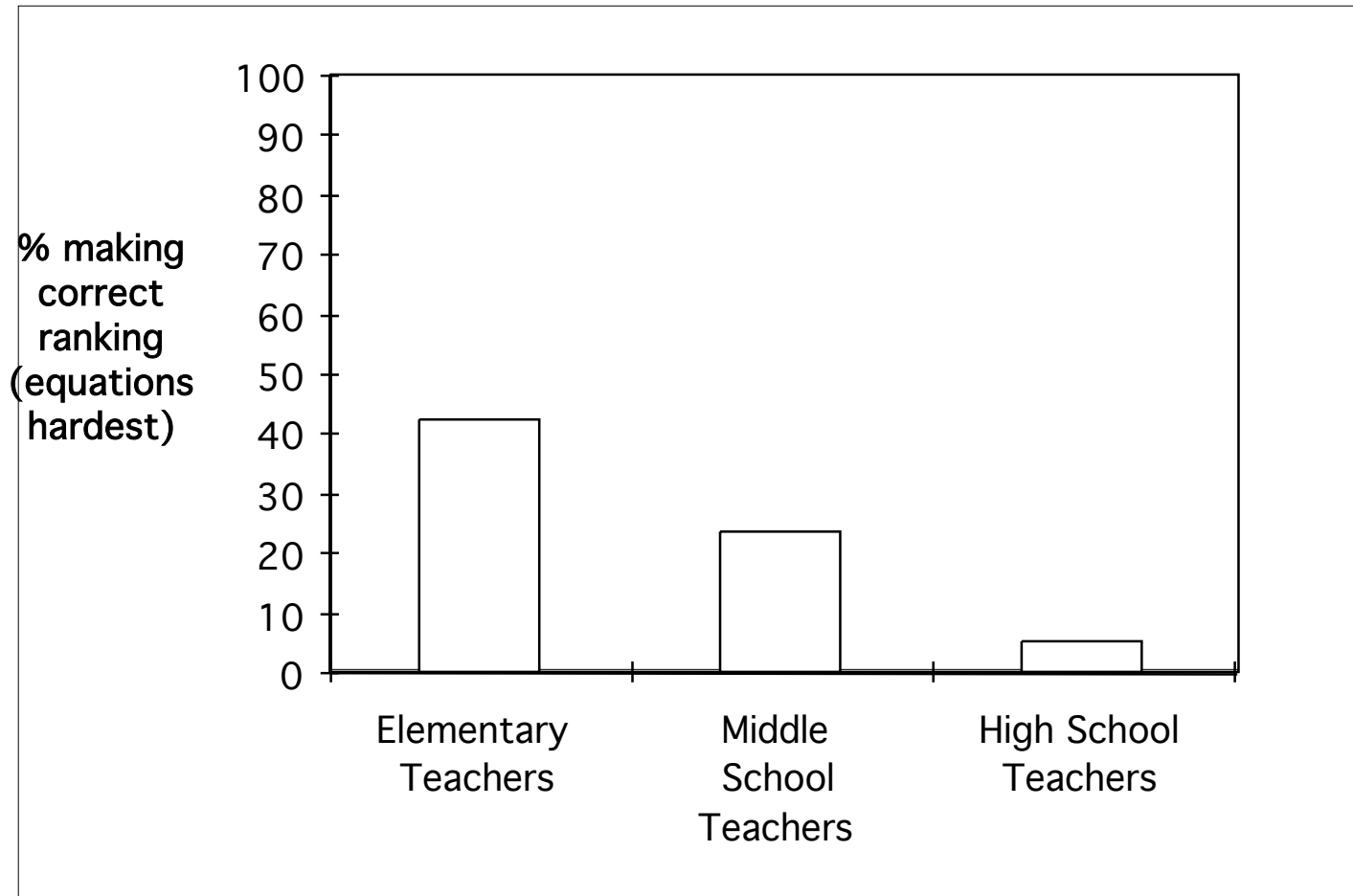
$$\begin{array}{r} 2.22 \\ +.59 \\ \hline 2.81 \end{array}$$

$$\boxed{2.81}$$



# Expert Blind Spot:

Expertise can impair judgment of student difficulties



Nathan, M. J. & Koedinger, K. R. (2000). An investigation of teachers' beliefs of students' algebra development. *Cognition and Instruction*, 18(2), 207-235

# What's behind expert blind spot?

- Blind spot results from limited memory of mostly implicit learning experiences
- Self-reflections on thinking are biased
  - More aware of verbally-mediated reasoning
    - More words => more thinking needed
  - Not aware of implicit processing & learning
    - Equations need to be “read” too
    - Fluent algebra language processing requires extensive implicit learning

# But, symbols do help for more complex problems ...

More complex *multiple-unknown* problems

## Story Problem

Roseanne just paid \$38.24 for new jeans. She got them at a 15% discount. What was the original price?

## Equation

$$X - 0.15X = 38.24$$

Koedinger, Alibali, & Nathan (2008). Trade-offs between grounded and abstract representations: Evidence from algebra problem solving. *Cognitive Science*.

# CTA used to design Algebra Cognitive Tutor & Text

**Analyze real world problem scenarios**

**scenario**

An experimental aircraft has sunk off the coast of South Africa at a depth of 12,790 feet. The military have located the aircraft and are in the process of raising it to the surface. It is currently 7625 feet below the surface and is being raised at the rate of 185 feet per hour. (Hint: Consider the direction above sea level to be positive)

- How deep was the aircraft five hours ago?
- How deep will the aircraft be five hours from now?
- When did the military start raising the aircraft?
- When will the aircraft reach the surface?

To write an expression, define a variable for the time from now and use this variable to write a rule for the depth of the aircraft.

**Use graphs, graphics calculator**

	Lower Bound	Upper Bound	Interval
TIME Settings	-5	15	1
DEPTH Settings	-15,000	0	1,000

**Use table, spreadsheet**

	TIME	DEPTH
Unit	HOURS	FEET
Expression	H	-7625+185H
1	-5	-8,550
2	5	-6,700
3	-27.9189...	-12,790

**Use equations, symbolic calculator**

$-7625+185H = -12790$

Add 7625

$185H = -5,165$

Divide by 185

$H = -1,033/37$

**Tracked by knowledge tracing**

- Changing axis bounds
- Changing axis intervals
- Correctly placing points
- Write expression, any form
- Find Y, any form
- Find X, any form
- Identifying units
- Entering a given

**Model tracing to provide context-sensitive Instruction**

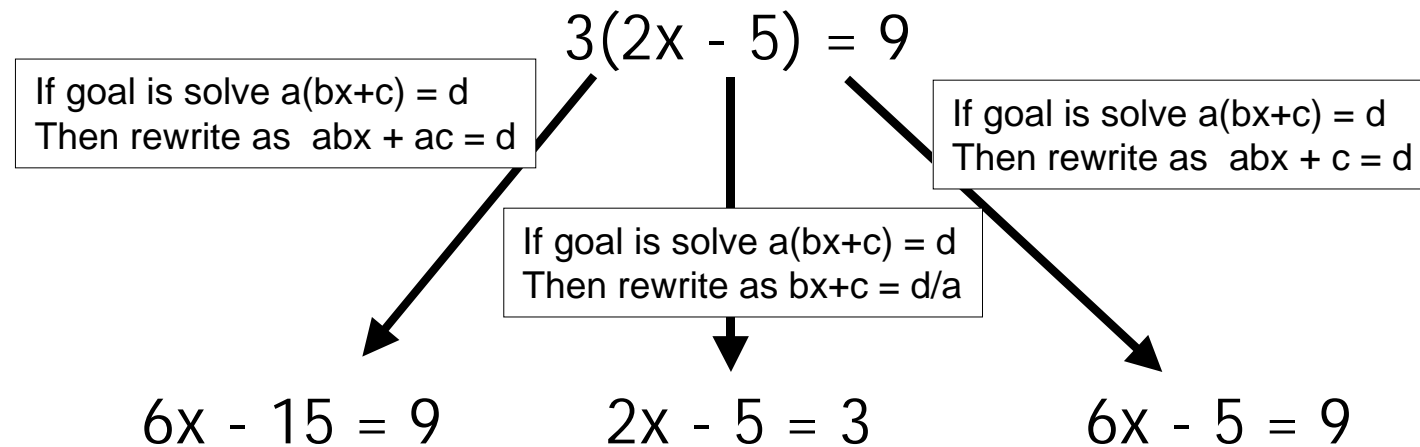
**Messages**

You have entered the given 0 in the wrong column of the worksheet.

# Cognitive Tutor Technology

Use cognitive model to individualize instruction

- Cognitive Model: A system that can solve problems in the various ways students can

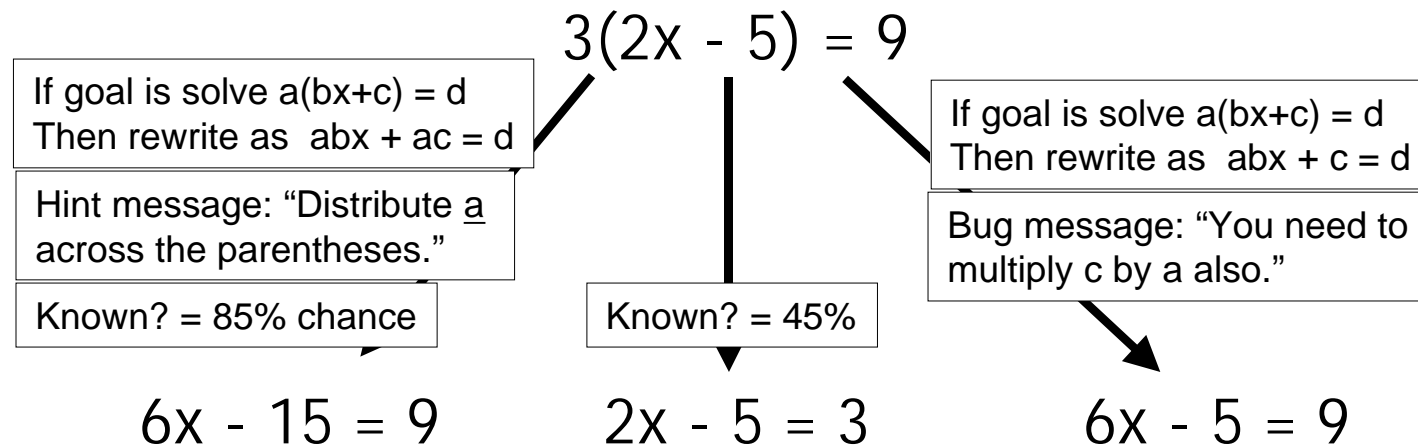


- Model Tracing: Follows student through their individual approach to a problem -> context-sensitive instruction

# Cognitive Tutor Technology

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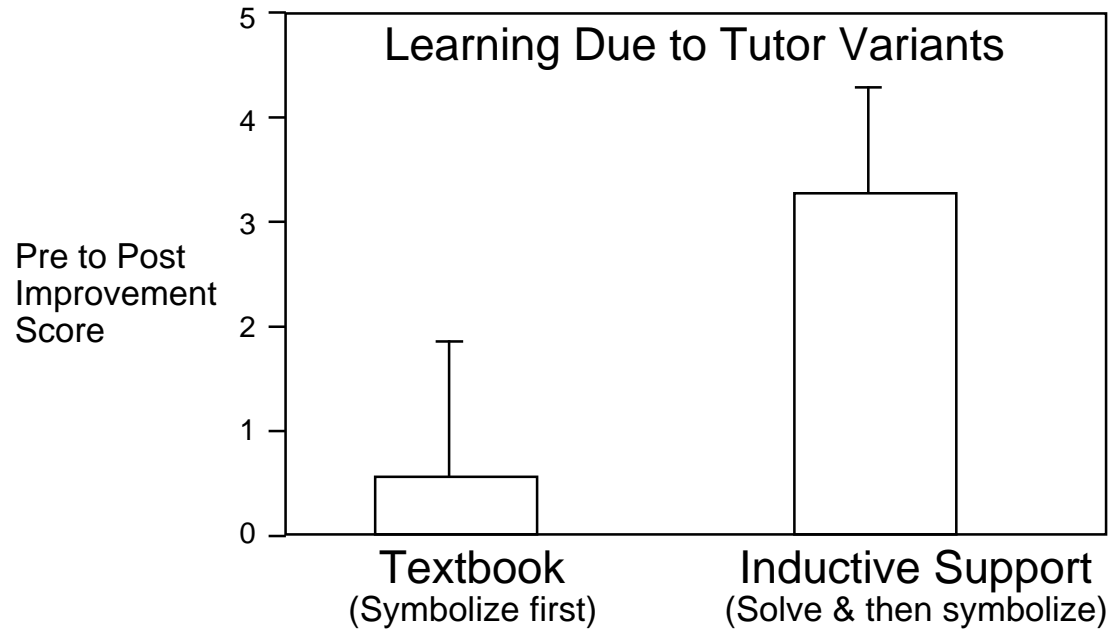


- Model Tracing: Follows student through their individual approach to a problem -> context-sensitive instruction
- Knowledge Tracing: Assesses student's knowledge growth -> individualized activity selection and pacing

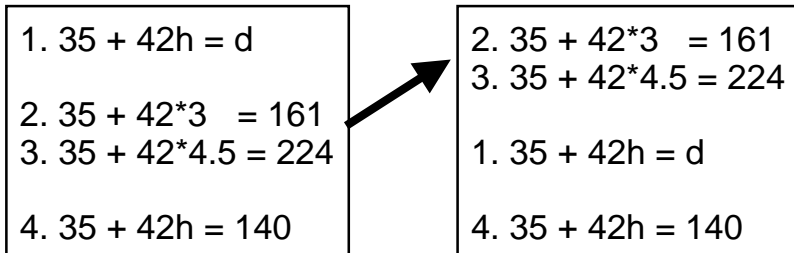
# *In vivo* experiments that close the loop

- How does knowledge analysis lead to improved instructional design?
- Performance aids may not be learning aids
- Example *in vivo* experiments
  - *Inductive support*: Have students generalize formalisms from concrete solutions
  - *Symbolic language practice*
- *In vivo*: Principle-testing (change one thing) experiments within real courses

# Parametric Study: Textbook vs. Cognitively-Based Design



Drane & Route Plumbing Co. charges \$42 per hour plus \$35 for the service call.



Koedinger, K. R., & Anderson, J. R. (1998). Illustrating principled design: The early evolution of a cognitive tutor for algebra symbolization. *Interactive Learning Environments*.



# Symbols & transfer

## Common views

- Math & language cognition are quite different
- Analog problems support transfer
- Problem schemas are induced

## Alternate view

- Elements of math learning engage language learning processing
- *Parts of solutions* can support transfer
- Modular hierarchical deep structure induced

# Seeing Language Learning Inside the Math: Cognitive Analysis Yields Transfer

Koedinger, K.R. & McLaughlin, E.A. (2010).  
*In Proceedings of the 32nd Annual Conference of the  
Cognitive Science Society.*

## Problem

Solution   %Correct\*

Original  
symbolization

Ann is in a rowboat on a lake. She is 800 yards from the dock. She then rows for  $m$  minutes back towards the dock. Ann rows at a speed of 40 yards per minute. Write an expression for Ann's distance from the dock.



800-40m

40%

with  
comprehension  
hints

Hint 1: Ann's distance from the dock is *equal* to the distance she started away from the dock *minus* the number of yards she rowed back toward the dock.  
Hint 2: The distance Ann has rowed is *equal* to the number of minutes *multiplied* by the number of yards per minute she rows.



800-40m

41%

Problem to solve

Ann is in a rowboat on a lake. She is 800 yards from the dock. She then rows for 3 minutes back towards the dock. Ann rows at a speed of 40 yards per minute. How far is Ann from the dock now?



680

63%

Decomposed

Ann #1: Ann is in a rowboat on a lake. She is 800 yards from the dock. She then rows  $y$  yards back towards the dock. Write an expression for Ann's distance from the dock.

Ann #2: Ann is in a rowboat on a lake. Ann rows for  $m$  minutes back towards the dock. She rows at a speed of 40 yards per minute. Write an expression for the distance Ann has rowed.



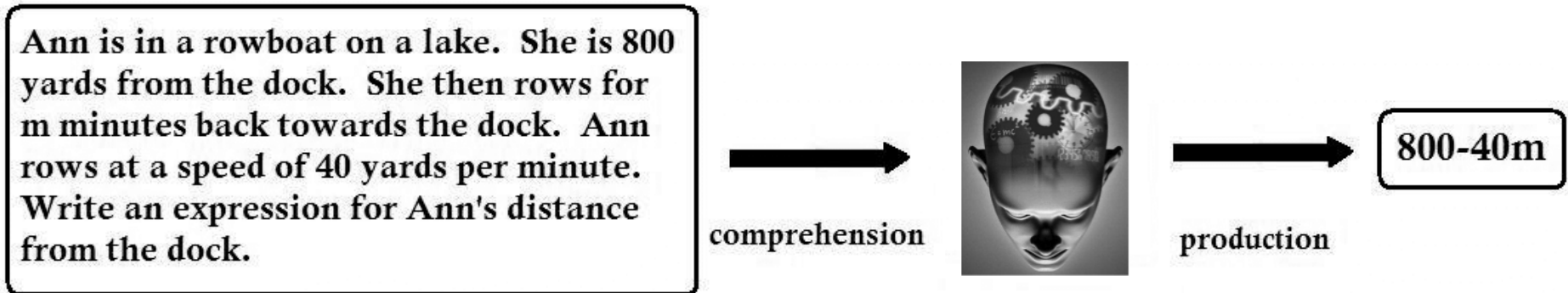
800-y

40m

62%

\* Heffernan & Koedinger, 1997

# What's hard about learning to symbolize?



Comprehension is not the key source of difficulty in translating story problems

Algebra is like a second language

In translating English to Greek, the hard part is not comprehending the English, but producing the Greek

Hypoth: Substitution practice will aid algebra grammar learning & transfer

**Substitute  $40 \cdot m$  for  $y$  in  $800 - y$   
Write the resulting expression.**

**Solution:  $800 - 40m$**

- Based on analogical transfer theory, such problems seem unlikely to help. Not similar to target problems.
- Alternatively, transfer may occur if
  - Probs support induction of recursive grammar patterns, like  $\text{expr} \Rightarrow \text{expr op expr}$

Target:

*2-step problem*

Ms. Lindquist is a math teacher. Ms. Lindquist teaches 62 girls. Ms. Lindquist teaches *f fewer boys* than girls. Write an expression for how many students Ms. Lindquist teaches.

Source  
options:

*1-step problem*

Ms. Lindquist is a math teacher. Ms Lindquist teaches 62 girls. Ms Lindquist teaches *b boys*. Write an expression for how many students Ms. Lindquist teaches.

*Substitution problem*

Substitute  $62 - f$  for  $b$  in  $62 + b$   
Write the resulting expression.

# Substitution practice transfers to symbolization

Condition	<i>n</i>	Pretest Mean (st error)	Instruct Mean (st error)	Filler Mean (st error)	Adj posttest Mean (st error)
1-step sym practice	154	.56 (.03)	.72 (.04)	.51 (.04)	.32 (.02)
Substitution practice	149	.57 (.03)	.52 (.04)	.72 (.04)	.39 (.02)

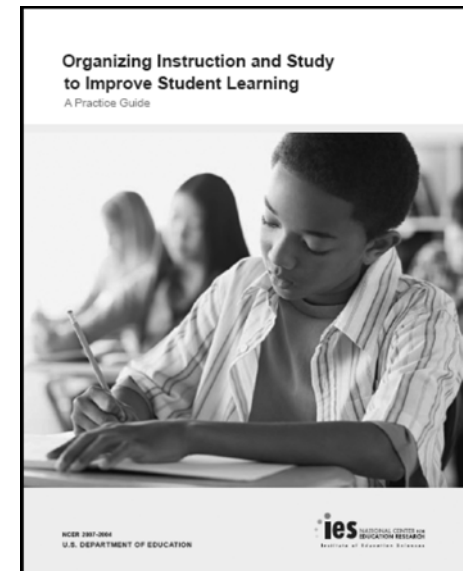
- Significant effect of condition ( $p < .05$ )
- Substitution transfers to story problems better than story problems themselves!
- Evidence for 1) algebra grammar  
2) decomposability of knowledge & instruction

# Two Paths To Effective Instructional Improvement

- Performing domain-specific cognitive task analysis
- *Applying domain-general principles of learning & instruction*

# What's the best form of instruction? Two choices?

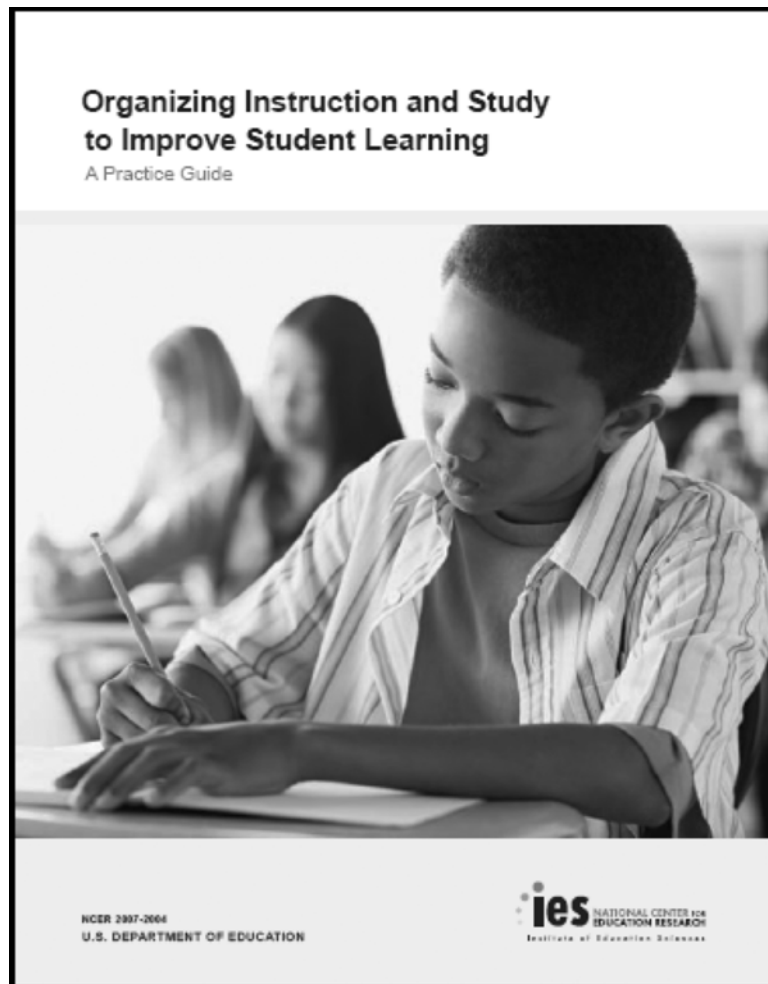
- More assistance vs. more challenge
  - Basics vs. understanding
  - Education wars in reading, math, science...
- Researchers like binary oppositions too. We just produce a lot more of them!
  - Massed vs. *distributed* (Pashler)
  - Study vs. *test* (Roediger)
  - *Examples* vs. problem solving (Sweller, Renkl)
  - *Direct instruction* vs. discovery learning (Klahr)
  - Re-explain vs. *ask for explanation* (Chi, Renkl)
  - *Immediate* vs. *delayed* (Anderson vs. Bjork)
  - *Concrete* vs. *abstract* (Pavio vs. Kaminski)
  - ...



Koedinger & Aleven (2007). Exploring the assistance dilemma in experiments with Cognitive Tutors. *Ed Psych Review*.



# Recommendations from DoE Practice Guide



## Recommendation 1: Space learning over time.



To help students remember key facts, concepts, and knowledge, we recommend that teachers arrange for students to be exposed to key course concepts on at least two occasions—separated by a period of several weeks to several months. Research has shown that delayed re-exposure to course material often markedly increases the amount of information that students remember. The delayed re-exposure to the material can be promoted through homework assignments, in-class reviews, quizzes (see Recommendation 3), or other instructional exercises. In certain classes, important content is automatically

## Recommendation 2: Interleave worked example solutions and problem-solving exercises.



When teaching mathematical or science problem solving, we recommend that teachers interleave worked example solutions and problem-solving exercises—literally alternating between worked examples demonstrating one possible solution path and problems that the student is asked to solve for himself or herself—because research has shown that this interleaving markedly enhances student learning.

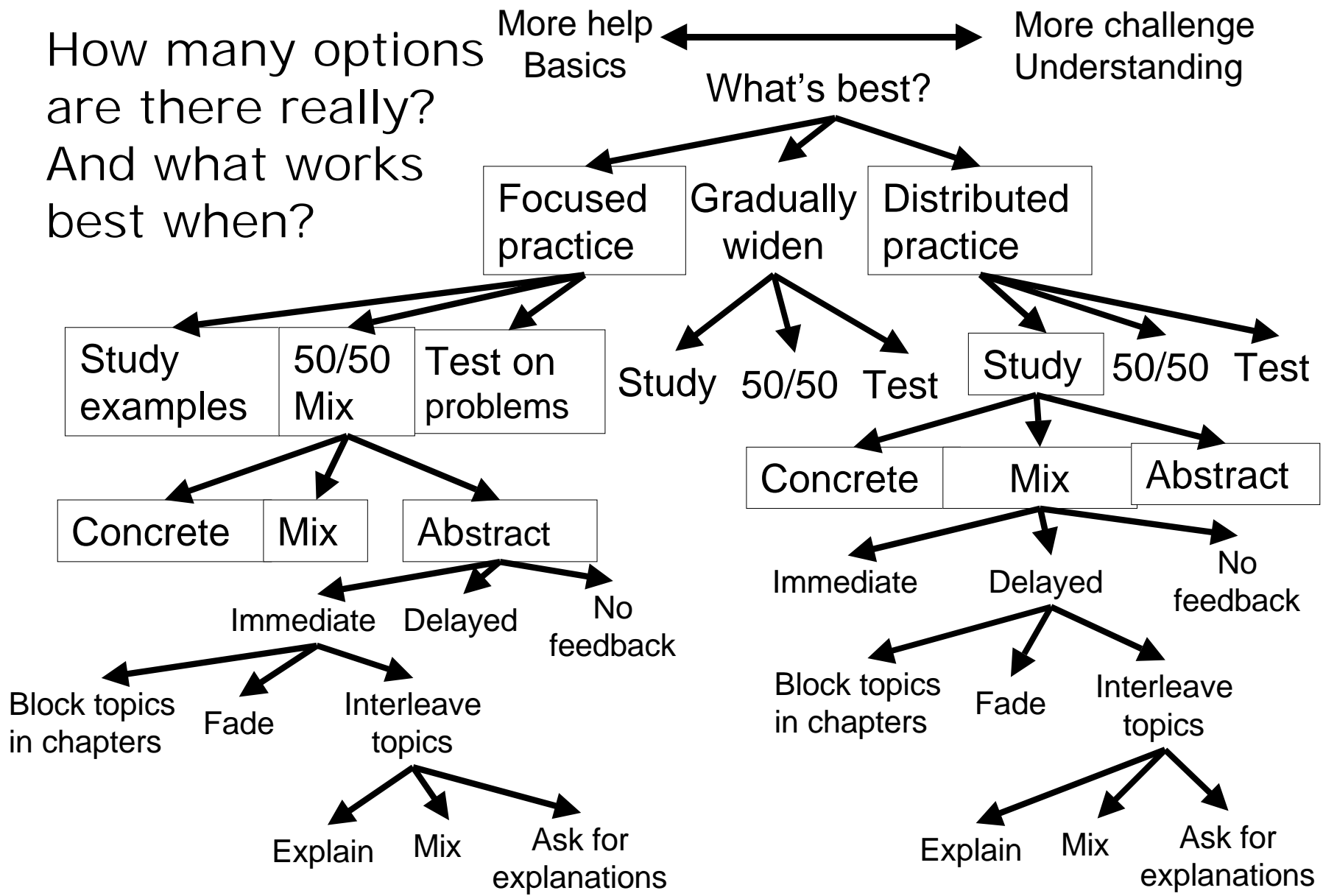
## Recommendation 7: Help students build explanations by asking and answering deep questions.



When students have acquired a basic set of knowledge about a particular topic of study and are ready to build a more complex understanding of a topic, we recommend that teachers find opportunities to ask questions and model answers to these questions, in order to help students build deep explanations of key concepts. By *deep* explanations we mean explanations that appeal to causal mechanisms, planning, well-reasoned arguments, and logic. Examples of deep explanations include those that inquire about causes and consequences of historical events, motivations of people involved in historical events, scientific evidence for particular theories, and logical justifications for the steps of a mathematical proof.

Examples of the types of questions that prompt deep explanations are *why*, *why-not*, *how*, *what-if*, *how does X compare to Y*, and *what is the evidence for X*? These questions and explanations can occur both during classroom instruction, class discussion, and during independent study.

How many options are there really?  
And what works best when?



Derivation:

- 15 instructional dimensions
  - 3 options per dimension
  - 2 stages of learning
- = >  $3^{15 \times 2}$  options

205,891,132,094,649

Center-level effort needed to  
tackle this complexity

Cumulative theory development

Field-based basic research with  
microgenetic data collection

# Many Pittsburgh Science of Learning Center studies in this space ...

- Researchers like binary oppositions too. We just produce a lot more of them!
  - Massed vs. *distributed* (Pashler)
  - Study vs. *test* (Roediger)
  - *Examples* vs. problem solving (Sweller, Renkl)
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  - ...

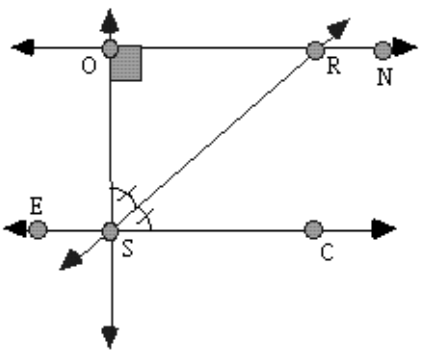
# Example *In Vivo* Experiment on “Self-Explanation”

- Self-explanation: Have students explain steps in solutions
- *In vivo* experiments: Tightly controlled principle-testing experiment embedded in a real course

Aleven, V. & Koedinger, K. R. (2002). An effective metacognitive strategy: Learning by doing and explaining with a computer-based Cognitive Tutor. *Cognitive Science*, 26(2)

# Explanation Treatment Condition (in computer tutor)

### External Angle & Parallel Lines



Given:  $ON \parallel EC$ . If the measure of Angle  $SOR$  is a right angle, find the measure of Angle  $SRN$ .

$m\angle SOR$	<input type="text" value="90"/>	Reason	<input type="text" value="given"/>
$m\angle OSC$	<input type="text" value="90"/>	Reason	<input type="text" value="int angles same side"/>
$m\angle OSR$	<input type="text" value="45"/>	Reason	<input type="text" value="angle bisection"/>
$m\angle ESR$	<input type="text" value="135"/>	Reason	<input type="text" value="angle addition"/>
$m\angle SRN$	<input type="text"/>	Reason	<input type="text"/>

### Messages

Some reasons dealing with parallel lines are highlighted in the Glossary. Which of these reasons is appropriate?

You can click on each reason in the Glossary to find out more.

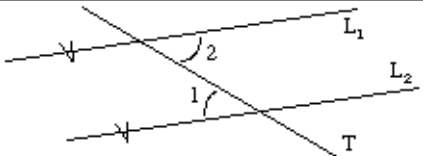
Problem solving answers

Explanation by reference

### Glossary

- Converse of Isosceles Triangle (Theorem)
- Isosceles Right Triangle
- Triangle Sum (Theorem)
- Linear Pair
- Linear Trio
- Parallel Lines --- Corr. Angles Are Cong**
- Parallel Lines --- Alt. Int. Angles Are C.**
- Parallel Lines --- Alt. Ext. Angles Are C.
- Parallel Lines --- Int. Angles on the Sa.

If two parallel lines are intersected by a transversal, then alternate interior angles are congruent.

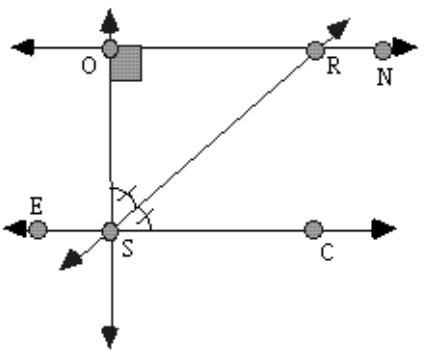


**Example:**  $L_1$  and  $L_2$  are parallel lines, intersected by transversal  $T$ .  $\angle 1$  and  $\angle 2$  are alternate interior angles. If  $m\angle 1$  is  $37^\circ$ , then  $m\angle 2$  is also  $37^\circ$ .

# Problem Solving Condition

## (Control: Computer Tutor as it was)

### External Angle & Parallel Lines



Given:  $ON \parallel EC$ . If the measure of Angle  $SOR$  is a right angle, find the measure of Angle  $SRN$ .

$m\angle SOR$    
 $m\angle OSC$    
 $m\angle OSR$    
 $m\angle ESR$    
 $m\angle SRN$

### Messages

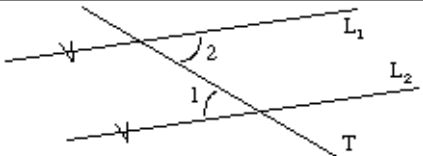
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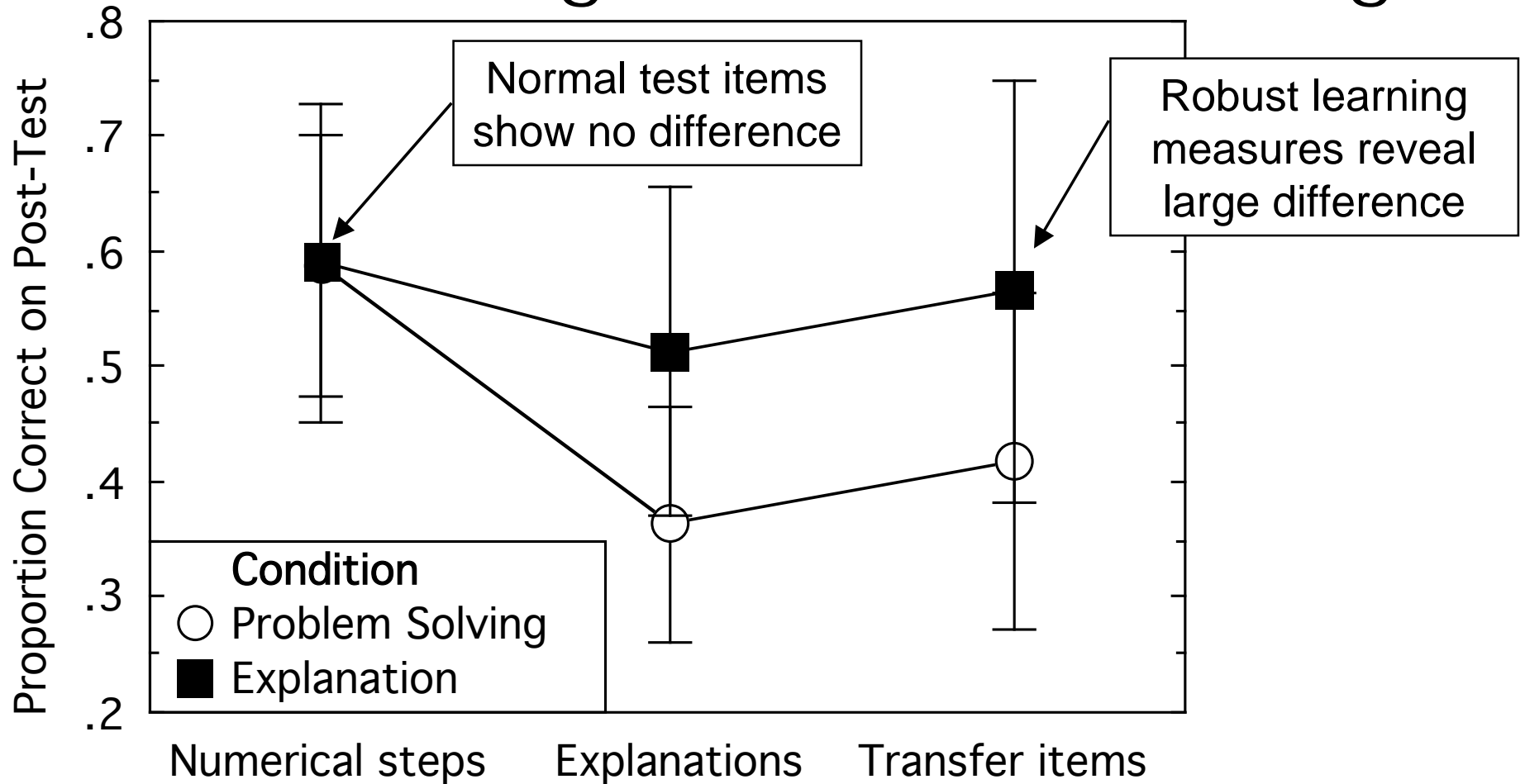
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# Self-explanation improves understanding => *robust* learning

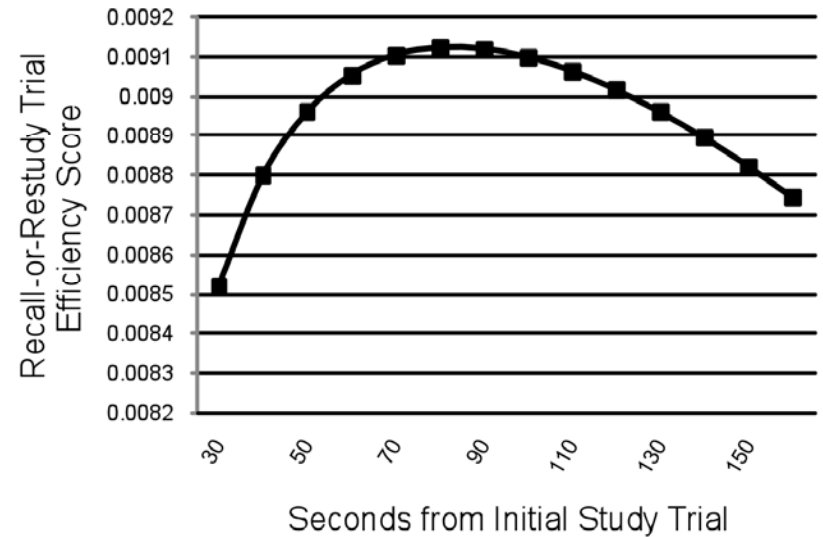


Aleven & Koedinger (2002). An effective metacognitive strategy: Learning by doing and explaining with a computer-based Cognitive Tutor. *Cognitive Science*.



# Assistance Formula

- Formalizing instructional decision-making
  - General principles combined with CTA
- How to best apply an instructional principle
  - Spacing, examples, ...
- Need data to set parameters



$$L = \frac{pS_b + (1 - p)F_b}{pS_c + (1 - p)F_c}$$

$L$  = long-term learning event efficiency  
 $p$  = probability of success  
 $S_b$  = long-term success benefit  
 $F_b$  = long-term failure benefit  
 $S_c$  = immediate success cost  
 $F_c$  = immediate failure cost

# Rational Cognitive Task Analysis: Tools for Computational Modeling

- SimStudent: A computational modeling of student learning
  - Teach it by demonstrating correct actions & giving feedback on incorrect actions
  - Learns external symbol use by induction
  - Quick demo?
- Find at [ctat.pact.cs.cmu.edu](http://ctat.pact.cs.cmu.edu)

Matsuda, Lee, Cohen, & Koedinger(2009). A computational model of how learner errors arise from weak prior knowledge. In *Proceedings of Cognitive Science Society*

# Modeling reveals many complications of learning & transfer

- SimStudent errors reveal many challenges to inducing generalized knowledge
  - Can make errors in generalizing *where* to find info, *how* & *when* to perform actions
- After seeing example:  $3x=9 \rightarrow x=3$ 
  - SimStudent successfully solves  $4x=16$  with  $x=4$
  - *How* error:  $5x=15 \rightarrow x=5$
  - After feedback on this one problem, now successful on  $7x=21$ ,  $10x=35$ , ...
- *When* error:  $x/5=10 \Rightarrow x=2$
- *Where* error: Gets stuck after  $7x+4=25 \rightarrow 7x=21$

# Summary

Two paths to improved instruction

1. Use CTA to uncover hidden keys to learning
    - Systematically collect student performance data to isolate KCs
  2. Employ general instructional principles
    - Much has been discovered: worked examples, comparison, self-explanation ...
    - But much more to discover
- Beware of assistance dilemmas =>  
Guide application of principles using CTA

# Non-verbal *learning* processes and verbal *instruction*

- Expert blind spot
  - We remember verbal instruction
  - We don't remember non-verbal learning processes that underlie much of expertise development
- Non-verbal learning processes include
  - Example-based induction/analogy, perceptual chunking & deep feature learning ...
- Verbal instruction influences non-verbal knowledge construction
  - Worked examples & deep questions focus limited cognitive resources on deeper thinking rather than shallow doing

# Conclusions

- Need more “learning by thinking”!
  - STEM class & homework is 95% problems, too much “learning by doing”
  - Should be 50% examples & deep questions
- We live with “learning” on a daily basis, but that doesn’t mean we understand it!
  - Need interdisciplinary science
    - to discover latent structure of domain knowledge
    - to better understand huge space of instructional options

*Thank you!*

